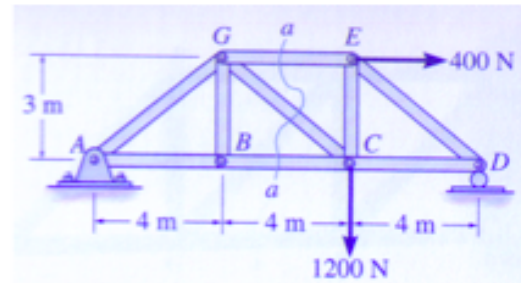


# Brief concept:

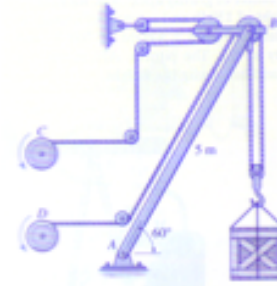
Frames and machines are defined as rigid bodies comprising of at least one multi-force member. **Frames are designed for supporting loads and usually stationary, while machines are designed to modify and transmit forces. It is very important to have a correct free body diagram.**

When drawing FBDs, it is useful to first identify two-force members and label of their unknowns. Doing this provides for less complicated FBDs, fewer equilibrium equations that need to be written and fewer unknowns to be determined.

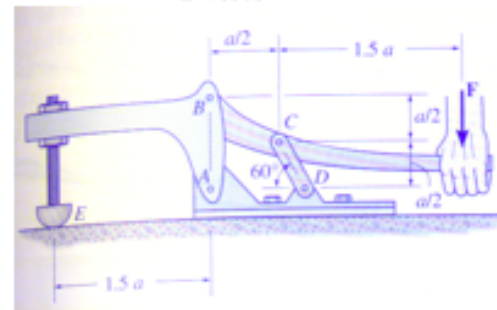
# Brief concept:



Trusses

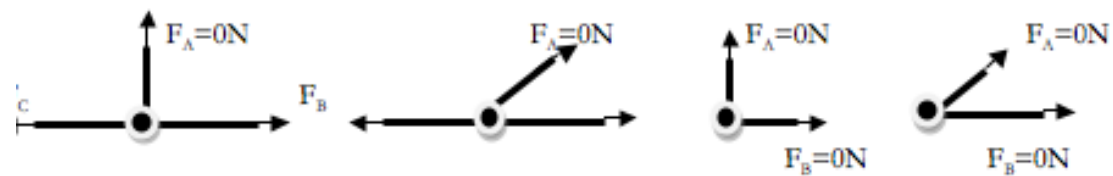


Frames



Machines

## ZERO-FORCE MEMBERS

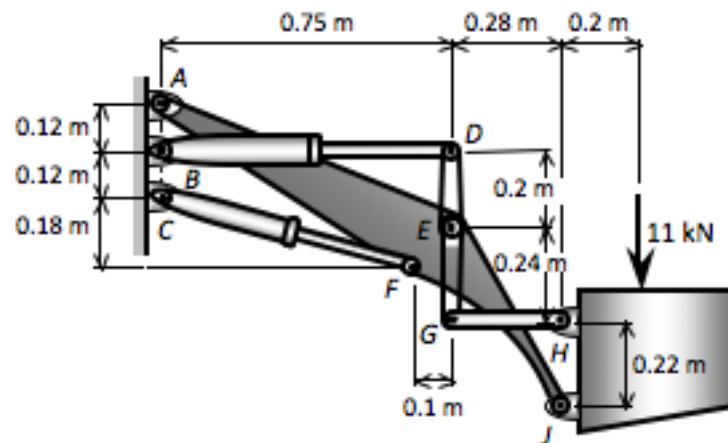


# Examples:

## EXAMPLE: MACHINES

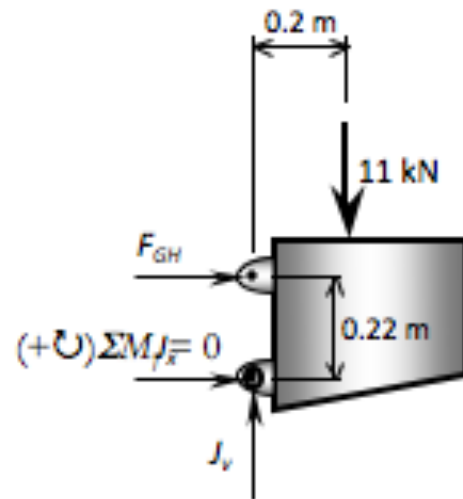
### QUESTION 1

Determine the force in hydraulic cylinders *BD* and *CF* for the mechanism shown in **Figure** to support the 11 kN load. State whether the cylinders are in tension or compression.



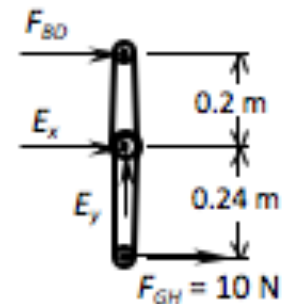
# Examples:

member HI



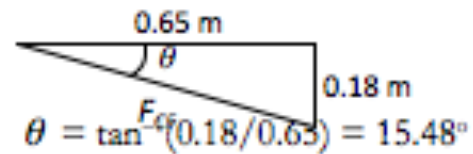
$$\begin{aligned}
 (+\curvearrowleft)\sum M_i &= 0 \\
 11(0.2) + F_{GH}(0.22) &= 0 \\
 F_{GH} &= -10 \text{ N} \\
 \therefore F_{GH} &= 10 \text{ N} \leftarrow \text{(tension)}
 \end{aligned}$$

member DEG



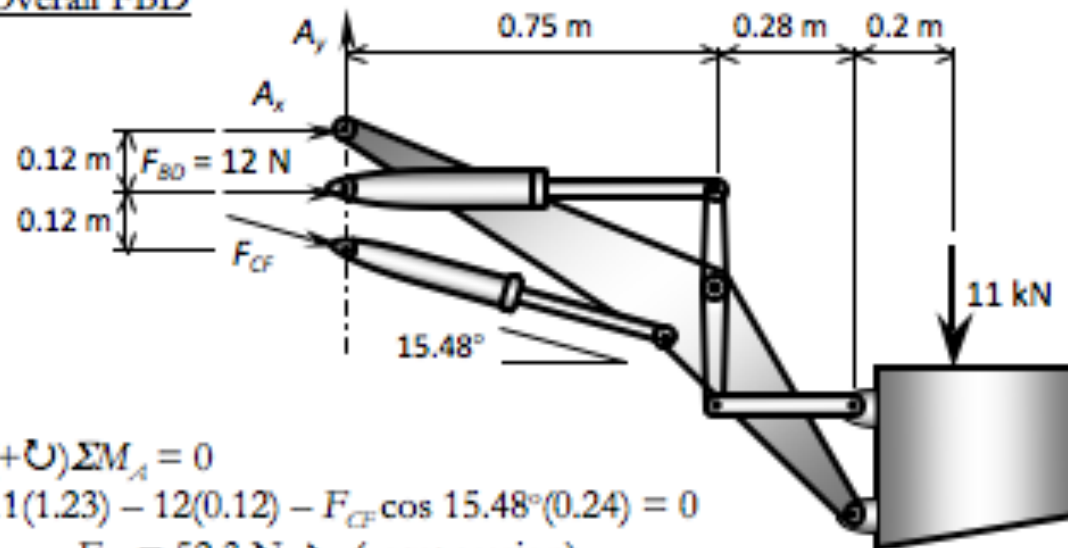
$$\begin{aligned}
 10(0.24) - F_{BD}(0.2) &= 0 \\
 F_{BD} &= 12 \text{ N} \rightarrow \text{(compression)}
 \end{aligned}$$

determine angle for  $F_{CF}$



# Examples:

Overall FBD



$$(+\curvearrowright) \Sigma M_A = 0$$

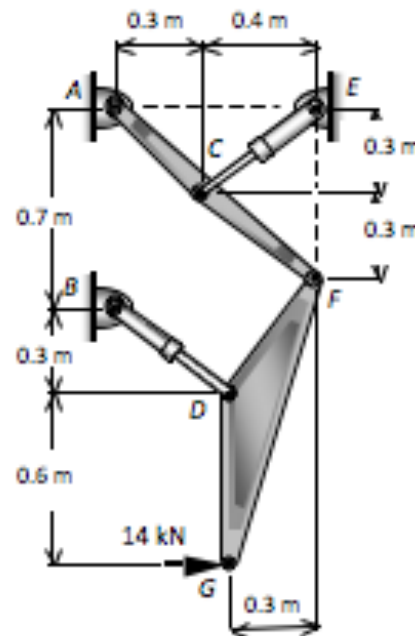
$$11(1.23) - 12(0.12) - F_{CF} \cos 15.48^\circ (0.24) = 0$$

$$F_{CF} = 52.3 \text{ N} \quad \searrow \text{ (compression)}$$

# Examples:

## QUESTION 2

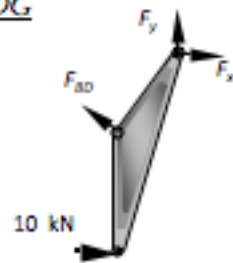
Determine components of the reaction at  $A$  and the force in hydraulic cylinders  $BD$  and  $CE$  when a  $14\text{ kN}$  force is applied at  $G$  of the mechanism shown in **Figure**. State whether the cylinders are in tension or compression.



# Examples:

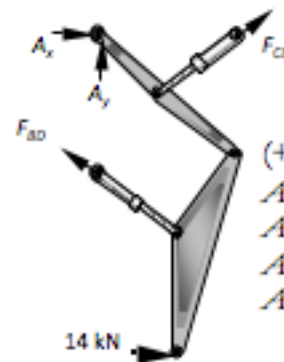
## Solution

### FDG



$$\begin{aligned}
 (+\curvearrowright) M_F &= 0 \\
 F_{BD} (4/5)(0.4) + F_{CE} (3/5)(0.3) - 14(1) &= 0 \\
 0.32 F_{BD} + 0.18 F_{BD} - 14 &= 0 \\
 F_{BD} &= 28 \text{ kN (T)}
 \end{aligned}$$

### Overall FBD

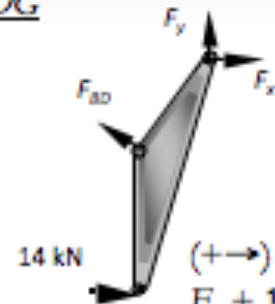


$$\begin{aligned}
 (+\curvearrowright) M_A &= 0 \\
 F_{BD} (4/5)(0.7) - F_{CE} (3/5)(0.7) - 14(1.6) &= 0 \\
 0.56(28) - 0.42 F_{CE} - 22.4 &= 0 \\
 F_{CE} &= -16 \text{ N (C)}
 \end{aligned}$$

$$\begin{aligned}
 (+\rightarrow) F_x &= 0 & (+\uparrow) F_y &= 0 \\
 A_x + F_{CE} (4/5) - 28(4/5) + 14 &= 0 & A_y + F_{CE} (3/5) + 28(3/5) &= 0 \\
 A_x + (-16)(4/5) - 28(4/5) + 14 &= 0 & A_y + (-16)(3/5) + 28(3/5) &= 0 \\
 A_x - 12.8 - 22.4 + 14 &= 0 & A_y - 9.6 + 16.8 &= 0 \\
 A_x &= 21.2 \text{ kN (}\rightarrow\text{)} & A_y &= -7.2 \text{ kN (}\downarrow\text{)}
 \end{aligned}$$

# Examples:

FDG

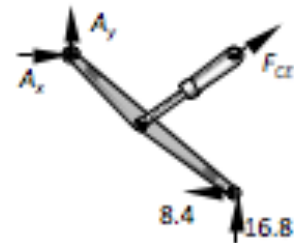


$$\begin{aligned}
 (+\rightarrow) F_x &= 0 \\
 F_x + 14 - 28(4/5) &= 0 \\
 F_x &= 8.4 \text{ kN } (\rightarrow)
 \end{aligned}$$

$$\begin{aligned}
 (+\curvearrowright) M_F &= 0 \\
 F_{BD} (4/5)(0.4) + F_{CE} (3/5)(0.3) - 14(1) &= 0 \\
 0.32 F_{BD} + 0.18 F_{BD} - 14 &= 0 \\
 F_{BD} &= 28 \text{ kN } (\text{T})
 \end{aligned}$$

$$\begin{aligned}
 (+\uparrow) F_y &= 0 \\
 F_y + 28(3/5) &= 0 \\
 F_y &= -16.8 \text{ kN } (\downarrow)
 \end{aligned}$$

ACF



$$\begin{aligned}
 (+\rightarrow) F_x &= 0 \\
 A_x - 16(4/5) - 8.4 &= 0 \\
 A_x &= 21.2 \text{ kN } (\rightarrow)
 \end{aligned}$$

$$\begin{aligned}
 (+\curvearrowright) M_A &= 0 \\
 8.4(0.6) - 16.8(0.7) - F_{CE}(3/5)(0.7) &= 0 \\
 5.04 - 11.76 - 0.42 F_{CE} &= 0 \\
 F_{CE} &= -16 \text{ N } (\text{C})
 \end{aligned}$$

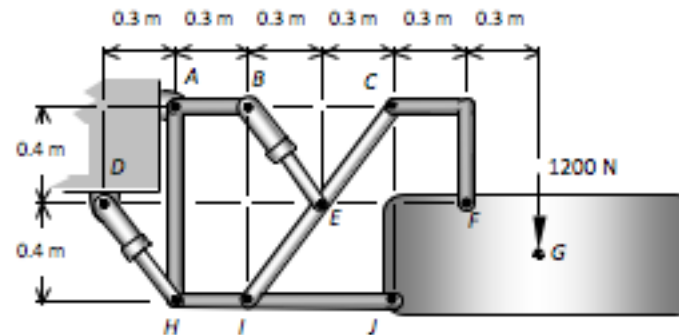
$$\begin{aligned}
 (+\uparrow) F_y &= 0 \\
 A_y - 16(3/5) + 16.8 &= 0 \\
 A_y &= -7.2 \text{ kN } (\downarrow)
 \end{aligned}$$



# Examples:

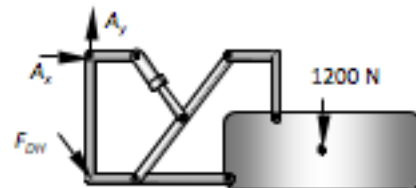
## QUESTION 3

The mechanism shown in **Figure** is used to support a 1200 N load at *G*. Determine components of the reaction at *A* and the force in hydraulic cylinders *DH* and *BE*, and state whether the cylinders are in tension or compression.

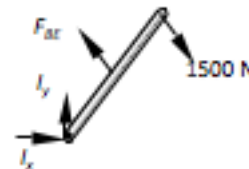


## Solution

### Overall FBD



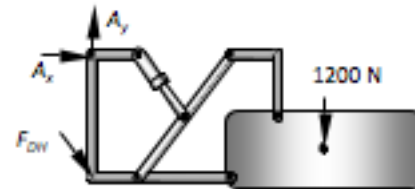
### IEC



# Examples:

## Solution

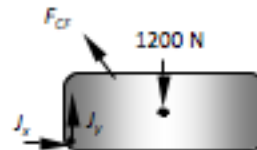
### Overall FBD



$$\begin{aligned}
 (+\curvearrowright) \quad M_A &= 0 \\
 1200(1.5) - F_{DH}(3/5)(0.8) &= 0 \\
 F_{DH} &= 3750 \text{ N (C)}
 \end{aligned}$$

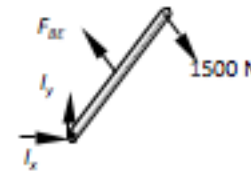
$$\begin{aligned}
 (+\rightarrow) \quad F_x &= 0 & (+\uparrow) \quad F_y &= 0 \\
 A_x + 3750(3/5) &= 0 & A_y - 3750(4/5) - 1200 &= 0 \\
 A_x &= -2250 & A_y &= 4200 \text{ N (\uparrow)} \\
 A_x &= 2250 \text{ N (\leftarrow)}
 \end{aligned}$$

### IEG



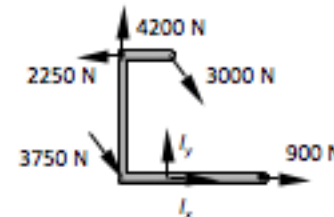
$$\begin{aligned}
 (+\curvearrowright) \quad M_J &= 0 \\
 1200(0.6) - F_{CF}(3/5)(0.4) - F_{CF}(4/5)(0.3) &= 0 \\
 720 - 0.24 F_{CF} - 0.24 F_{CF} &= 0 \\
 F_{CF} &= 1500 \text{ N (T)}
 \end{aligned}$$

### IEC



$$\begin{aligned}
 (+\curvearrowright) \quad M_I &= 0 \\
 1500(3/5)(0.8) + 1500(4/5)(0.6) \\
 - F_{BE}(3/5)(0.4) - F_{BE}(4/5)(0.3) &= 0 \\
 720 + 720 - 0.24 F_{BE} - 0.24 F_{BE} &= 0 \\
 F_{CF} &= 3000 \text{ N (T)}
 \end{aligned}$$

### check using BAHJJ

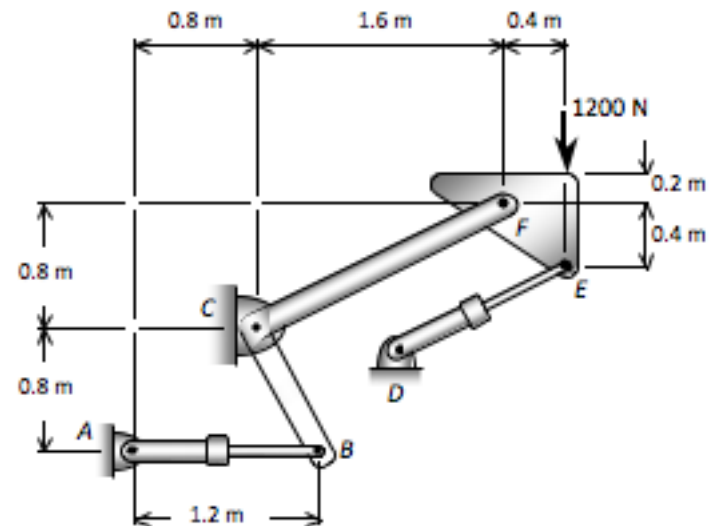


$$\begin{aligned}
 (+\curvearrowright) \quad M_J &= 0 \\
 3000(3/5)(0.8) - 2250(0.8) \\
 + 4200(0.3) - 3750(4/5)(0.3) &= 0 \\
 1440 - 1800 + 1260 - 900 &= 0
 \end{aligned}$$

# Examples:

## QUESTION 4

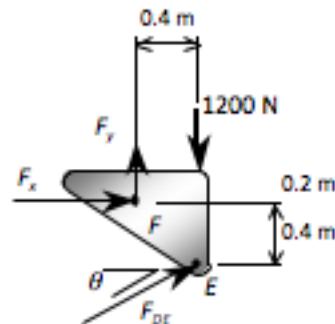
The mechanism shown in **Figure** is used to support the 1200 N load. Determine the force in the two identical hydraulic cylinders  $AB$  and  $DE$ , and components of the reaction at pin  $C$  for the system to maintain equilibrium. Hydraulic cylinder  $DE$  is parallel to  $CF$ .



# Examples:

## Solution

### FE



$$(+\curvearrowright) M_F = 0$$

$$1200(0.4) - F_{DE} \sin \theta (0.4) - F_{DE} \cos \theta (0.4) = 0$$

$$\theta = 10.816^\circ = 26.6^\circ$$

$$480 - 0.1791 F_{DE} - 0.358 F_{DE} = 0$$

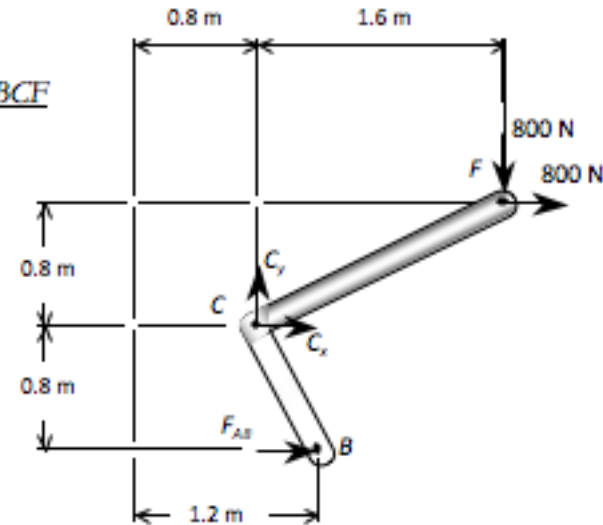
$$F_{DE} = 894 \text{ N}$$

$$(+\rightarrow) F_x = 0 \quad (+\uparrow) F_y = 0$$

$$F_x + F_{DE} \cos \theta = 0 \quad F_y - 1200 + F_{DE} \sin \theta = 0$$

$$F_x = -800 \text{ N } (\leftarrow) \quad F_y = 800 \text{ N } \uparrow$$

### BCF



$$(+\curvearrowright) M_C = 0$$

$$800(0.8) + 800(1.6) - F_{AB}(0.8) = 0$$

$$640 + 1280 - 0.8 F_{AB} = 0$$

$$F_{AB} = 2400 \text{ N}$$

$$(+\rightarrow) F_x = 0 \quad (+\uparrow) F_y = 0$$

$$C_x + 800 + 2400 = 0 \quad C_y - 800 = 0$$

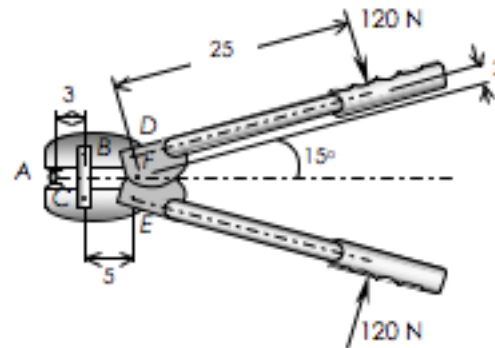
$$C_x = -3200 \text{ N } (\leftarrow) \quad C_y = 800 \text{ N } \uparrow$$

# Exercises:

## EXERCISE: MACHINES

### QUESTION 1

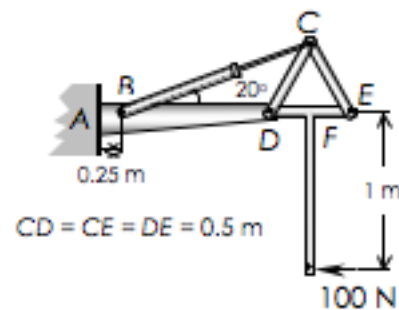
120 N forces are exerted on wire cutter as shown. Determine the forces acting on the wire. All dimensions in cm. ( $A = 5659\text{N}$ )



### QUESTION 2

The mechanism shown in the figure is used to support the 100 N load at G. Determine the force acting on the two force member  $CE$  and the hydraulic cylinder  $BC$  for this instant.

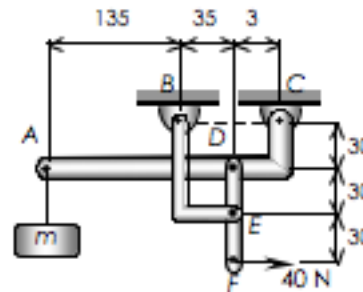
( $F_{CE} = 231\text{N (T)}$ ,  $F_{BC} = 311\text{N (T)}$ )



# Exercises:

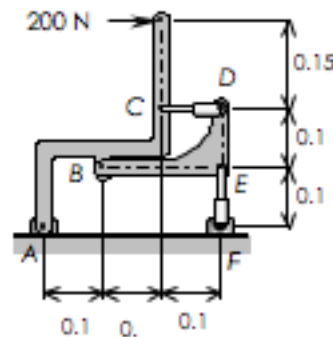
## QUESTION 3

The frame in the figure is used to support the mass  $m$  at end  $A$ . Determine the mass  $m$  (in kg) if a 40 N force is applied at  $F$ . All dimensions in cm. ( $m = 2.71\text{kg}$ )



## QUESTION 4

The mechanism shown is used to support the 200 N horizontal force at  $D$  by adjusting hydraulic cylinders  $CE$  and  $FG$ . Determine all components of forces acting on member  $ABC$  for the position shown. All dimensions in metres. ( $A_x = 200\text{N}(<)$ ,  $A_y = 233\text{N}(\wedge)$ ,  $B_x = 47\text{N}(>)$ ,  $B_y = 233\text{N}(\wedge)$ ,  $F_{CD} = 47\text{N}(\text{C})$ )



# Exercises:

## QUESTION 5

The figure shows a 180 kg adjustable platform  $AB$  used to raise a 550 kg crate with centre of gravity at  $G$ . Determine the force in the two-force member  $BC$  and hydraulic cylinder  $DF$  and state whether they are in tension or compression. All dimensions in cm. ( $F_{BC} = 2656\text{N}$  (C),  $F_{DF} = 5825\text{N}$  (C))

